II PU BASIC MATHEMATICS - 2024 75 (NS)

(English Version)

Instructions:

- The question paper has 5 parts namely, A, B, C, D and E. 1. Answer ALL the Parts.
- 2. Part - A carries 20 marks

Part – B carries 12 marks

Part – C carries 15 marks

Part – D carries 25 marks

Part – E carries 8 marks.

- 3. For Part - A questions, only the first written answers will be considered for evaluation.
- 4. In the Part - D, use graph sheet for the question number 40 on L.P.P.
- 5. Write the question numbers properly as indicated in the question paper.
- For question having graph, alternate question is given at 6. the end of the question paper in a separate section in the Part - F for Visually Challenged Students.

PART - A

Answer all the multiple choice questions:

 $(5 \times 1 = 5)$

1) If
$$A = \begin{bmatrix} 1 & 2 & 4 \\ -1 & 3 & -2 \end{bmatrix}$$
 and $B = \begin{bmatrix} 3 & -4 & -1 \\ 1 & 5 & -2 \end{bmatrix}$ then $(A+B)$ is

a)
$$\begin{bmatrix} 4 & 2 & -3 \\ 0 & 8 & 4 \end{bmatrix}$$

b)
$$\begin{bmatrix} 4 & -2 & 3 \\ 0 & 8 & -4 \end{bmatrix}$$

c)
$$\begin{bmatrix} -4 & 2 & 3 \\ 0 & -8 & 4 \end{bmatrix}$$

d)
$$\begin{bmatrix} 4 & -2 & -3 \\ 0 & -8 & -4 \end{bmatrix}$$

- 2) If ${}^{n}C_{10} = {}^{n}C_{15}$ then *n* is
 - . a) 25

b) 29

c) 24

- d) 23
- 3) The probability of getting a black card from a pack of 52 cards is

b) $\frac{1}{52}$

- d) $\frac{1}{2}$
- 4) The value of $4\cos^3 10^\circ 3\cos 10^\circ$ is
 - a) $\frac{\sqrt{3}}{2}$

- The value of $\int 4 \sec^2 x \, dx$ is 5)
 - $4 \sec x + c$

b) $4\sin x + c$

 $4 \tan x + c$

 $4 \cot x + c$ d)

II. Match the following :

$$(5 \times 1 = 5)$$

- 6) i) The value of $\begin{vmatrix} 3200 & 3201 \\ 3202 & 3203 \end{vmatrix}$ is
- a) 27

ii) If ${}^{5}P_{r} = 60$, then r is

- b) 12
- iii) If 5:20=3:x then the value of x is
- c) $\frac{y}{x}$
- iv) The value of $\lim_{x \to 3} \left(\frac{x^3 27}{x 3} \right)$ is
- d) $\frac{x}{y}$

v) If $x^2 - y^2 = a^2$ then $\frac{dy}{dx}$ is

- e) –2
- f) 3
- III. For question numbers 7 to 11 choose the appropriate answers from the brackets given below: $(5 \times 1 = 5)$

$$(56, 9, \frac{-3}{4}, 1, 2, 4)$$

7) If
$$\begin{bmatrix} 2 & x & 2 \end{bmatrix} \begin{bmatrix} 1 \\ 4 \\ 2 \end{bmatrix} = \begin{bmatrix} 3 \end{bmatrix}$$
 then the value of x is ————

8) The number of triangles that can be formed from the 8 non collinear points is



- 9) The third proportional of 4 and 6 is ————
- 10) The value of $\lim_{x\to 0} \left(\frac{\sin 4x}{\sin 2x}\right)$ is ______
- 11) The value of $\int_{0}^{\pi/2} \sin 2x \, dx$ is ————
- IV. Answer the following questions:

$$(5\times 1=5)$$

- 12) Negate: $\sim p \rightarrow q$
- 13) If a:b=2:3, b:c=5:7 and c:d=3:1 then find a:d.
- 14) If $\tan A = \frac{1}{\sqrt{3}}$ then find $\tan 2A$.
- 15) Differentiate $3x^2 + 4y^2 = 10$ w. r. t. x.
- 16) Evaluate $\int \left(x^2 \frac{6}{x} + 5e^x\right) dx$.



PART - B

V. Answer any six of the following questions:

 $(6 \times 2 = 12)$

- 17) In how many ways can the letters of the word "HOPPER" be arranged?
- 18) Find the number of parallelograms that can be formed from the set of 6 parallel lines intersecting another set of 4 parallel lines.
- 19) Two coins are tossed simultaneously. What is the probability of getting
 - a) Atleast one tail
 - b) Atmost one tail?
- 20) Divide ₹ 6,000 in the ratio 3 : 4 : 5.
- 21) 500 workers can finish a work in 8 days. How many workers will finish the same work in 5 days?
- 22) For ₹ 512.50 due 6 months at 15% p.a. Find the true present value and discounted value of the bill.
- 23) Find the equation of the parabola given that its focus is (-4,0) and directrix is x=4.

- 24) Find the axis and length of the latus rectum of the parabola $x^2 = 16 y$.
- 25) Evaluate $\int \frac{4x+3}{2x^2+3x+5} dx$.
- 26) Evaluate $\int_{0}^{3} \left(\frac{x+3}{x+2} \right) dx$.
- 27) Find the area enclosed by the curve $y = x^2$, x-axis and the ordinates x=0 and x=1.

PART - C

VI. Answer any five of the following questions:

 $(5 \times 3 = 15)$

28) Solve:

$$3x + 2y = 8$$
 and

$$4x - 3y = 5$$

by Cramer's rule.

- 29) The difference between BD and TD on a certain sum of money due in 6 months is ₹ 27. Find the amount of the bill if the rate of interest is 6% p.a.
- 30) A person invests ₹ 15,000 partly in 3% stock at 75 and partly in 6% stock at 125. If the income from both is ₹ 675. Find his investment in 2 types of stocks.



- 31) The price of a T.V set inclusive of sales tax of 9% is ₹ 13,407. Find its marked price. If the sales tax is increased to 13%, how much more does the customer pay for the T.V?
- 32) Find $\frac{dy}{dx}$, given that $x = a\cos^4 \theta$, $y = a\sin^4 \theta$.
- 33) A ladder of 15 feet long leans against a smooth vertical wall. If the top slides downwards at the rate of 2 ft/sec. Find how fast the lower end is moving when the lower end is 12 ft away from the wall.
- 34) Evaluate $\int \frac{x+2}{(2x-1)(x-3)} dx$.

PART - D

VII. Answer any five questions:

 $(5 \times 5 = 25)$

35) Solve the linear equations by matrix method.

$$x+y-z=1$$

$$3x+y-2z=3$$

$$x-y-z=-1$$

- 36) Find the coefficient of x^8 in $\left(3x^2 \frac{1}{2x}\right)^{10}$.
- 37) Resolve $\frac{2x^2 + 10x 3}{(x+1)(x-3)(x+3)}$ into partial fractions.
- 38) Show that $\sim (p \vee q) \rightarrow (\sim p \wedge \sim q)$ is a Tautology.

- 39) ABC company required 1000 hours to produce 1st 30 engines. If the learning effect is 90%. Find the total labour cost at ₹ 20/hour to produce a total of 120 engines.
- 40) Solve the following LPP graphically.

Maximize: Z = 5x + 3y

Subject to the constraints:

$$3x + 5y \le 15$$
,

$$5x + 2y \le 10$$
,

$$x \ge 0$$
,

$$y \ge 0$$
.

41) Prove that :

$$\frac{\sin 6A + \sin 2A + 2\sin 4A}{\sin 7A + \sin 3A + 2\sin 5A} = \frac{\sin 4A}{\sin 5A}.$$

- 42) Find the equation of the circle passing through the points (1, -4), (5, 2) and having its centre on the line x-2y+9=0.
- 43) Evaluate $\lim_{x\to 2} \left[\frac{x^2-4}{\sqrt{x+2}-\sqrt{3x-2}} \right]$.

PART - E

VIII. Answer any two of the following questions:

$$(2\times 4=8)$$

- 44) A flag staff stands upon the top of a building at a distance of 20 mts. The angles of elevation of the top of the flag staff and the building are 60° and 30° respectively. Find the height of the flag staff.
- 45) If $y = a\cos(\log x) + b\sin(\log x)$ show that $x^2y_2 + xy_1 + y = 0$.



- 46) The total revenue function is given by $R = 400 x 2x^2$ and the total cost function is given by $C=2x^2+40x+4000$. Find
 - a) The marginal revenue and marginal cost functions.
 - b) The output at which marginal revenue = marginal cost.

PART - F

 $(1\times 5=5)$ (Only for Visually Challenged Students)

40) Smaran being a manufacturer of nuts and bolts for industrial machinery. It takes 1 hour of work on machine A and 3 hours on machine B to produce a package of nuts while it takes 3 hours on machine A and 1 hour on machine B to produce a package of Bolts. He earns a profit of ₹ 2.50/package of nuts and ₹ 1/package of bolts. Form a linear programming problem to maximise his profit, if he operates each machine for atmost 12 hours a day.